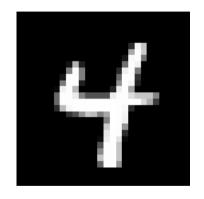
DSC 1408 Representation Learning

Lecture 16 | Part 1

Convolutions

H(x) = W, x, twexz + ... + Waxa + Wo



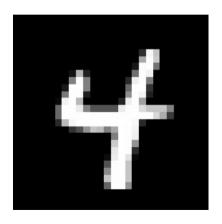
```
/+ —— + /
```

From Simple to Complex

- Complex shapes are made of simple patterns
- The human visual system uses this fact
- ▶ Line detector → shape detector → ... → face detector
- Can we replicate this with a deep NN?

Edge Detector

- How do we find vertical edges in an image?
- One solution: convolution with an edge filter.



Vertical Edge Filter

D	-/	/
0	1	/
0	-/	1

Idea
$$0 + (-10) + 60 + (-10) +$$

- Take a patch of the image, same size as filter.
- Perform "dot product" between patch and filter.
- If large, this is a (vertical) edge.





Idea
$$0+0+0+0+0+0+10+=0$$

Take a patch of the image, same size as filter.

- Perform "dot product" between patch and filter.
- If large, this is a (vertical) edge.





Idea
$$0+0+0+1 \\ 0+0+.9 \\ = 1.8$$

Move the filter over the entire image, repeat procedure.

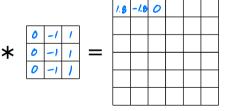
0	0	0	0	0	0						
0	0	.9	0	0	.7					1.8	
0	0	.9	0	0	.8						
0	0	.8	0	0	.9		J.	0 -1 1	_		
0	0	.7	0	0	0		*	0 -1 1	=		
								0 -1 1			

Move the filter over the entire image, repeat procedure.

0 0 0 0	0 0 0 0	0 .9 .9 .8 .7	0 0 0 0	0 0 0 0	0 .7 .8 .9			* \(\begin{array}{c c c c c c c c c c c c c c c c c c c	/	1.8	-1.8				
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Move the filter over the entire image, repeat procedure.

0	0	0	0	0	0	
0	0	.9	0	0	.7	
0	0	.9	0	0	.8	
0	0	.8	0	0	.9	
0	0	.7	0	0	0	



Move the filter over the entire image, repeat procedure.

0	0	0	0	0	0	
0	0	.9	0	0	.7	
0	0	.9	0	0	.8	
0	0	.8	0	0	.9	
0	0	.7	0	0	0	

		1.8	-1.8	0		
	1	2.6				
0 -1 1	_					
0 -/ /	=					
0 51 /						

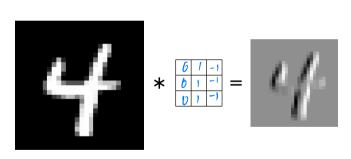
Move the filter over the entire image, repeat procedure.

0	0	0	0	0	0]				
0	0	.9	0	0	.7						
0	0	.9	0	0	.8			٦			
0	0	.8	0	0	.9		4	┤_			
0	0	.7	0	0	0		*	- −			
								_			

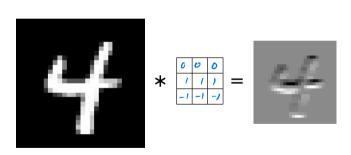
Convolution

- ► The result is the (2d) **convolution** of the filter with the image.
- Output is also 2-dimensional array.
- Called a response map.

Example: Vertical Filter



Example: Horizontal Filter

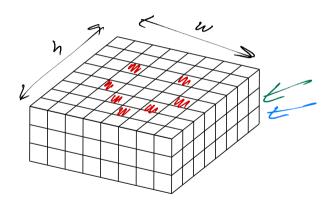


More About Filters

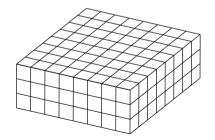
- ► Typically 3×3 or 5×5.
- ► Variations: different **stride**, image **padding**.

- Black and white images are 2-d arrays.
- But color images are 3-d arrays:
 - a.k.a., tensors
 - ► Three color **channels**: red, green, blue.
 - ► height × width × 3
- ► How does convolution work here?

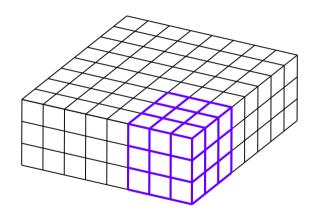
Color Image

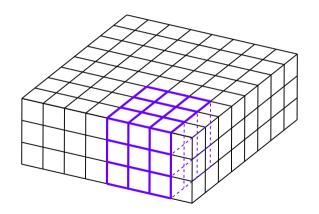


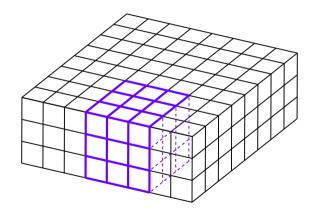
- ► The filter must also have three channels:
 - \triangleright 3 × 3 × 3, 5 × 5 × 3, etc.











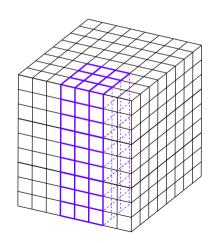
Convolution with 3-d Filter

- Filter must have same number of channels as image.
 - ▶ 3 channels if image RGB.

Result is still a 2-d array.

General Case

- ► Input "image" has *k* channels.
- Filter must have *k* channels as well.
 - ► e.g., 3 × 3 × k
- ► Output is still 2 d



DSC 1408 Representation Learning

Lecture 16 | Part 2

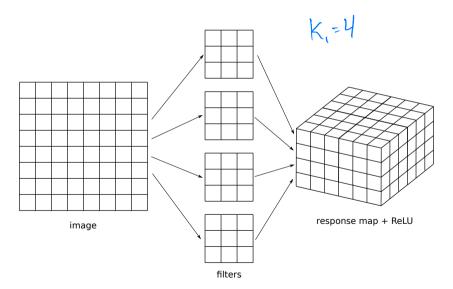
Convolutional Neural Networks

Convolutional Neural Networks

CNNs are the state-of-the-art for many computer vision tasks

- ► **Idea**: use convolution in early layers to create new feature representation.
- But! Filters are learned.

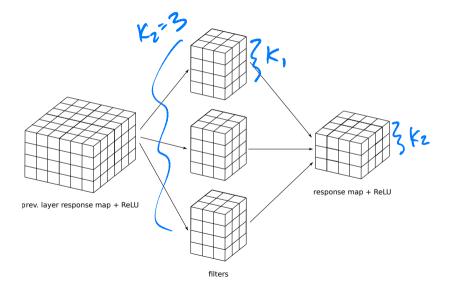
Input Convolutional Layer



Input Convolutional Layer

- Input image with one channel (grayscale)
- ► k_1 filters of size $\ell \times \ell \times 1$
- Results in k_1 convolutions, stacked to make response map.
- ReLU (or other nonlinearity) applied entrywise.

Second Convolutional Layer



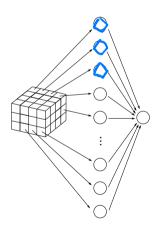
Second Convolutional Layer

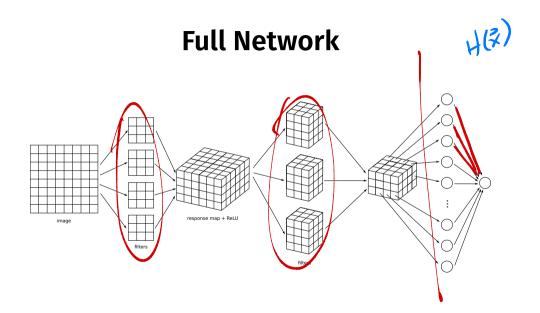
- Input is a 3-d tensor.
 - ▶ "Stack" of k_1 response maps.
- \triangleright k_2 filters, each a 3-d tensor with k_1 channels.
- \triangleright Output is a 3-d tensor with k_2 channels.

More Convolutional Layers

- May add more convolutional layers.
- Last convolutional layer used as input to a feedforward, fully-connected network.
- Need to "flatten" the output tensor.

Flattening





What is learned?

- ► The filters themselves.
- ► The weights in the feedforward NN used for prediction.

Max Pooling

- Max pooling is an important part of convolutional layers in practice.
- Reduces size of response map, number of parameters.

20	30	10	5	
10	15	20	36	
5	2	10	7	
			Ţ	

DSC 1408 Representation Learning

Lecture 16 | Part 3

Example: Image Classification





















d=32.32



Details

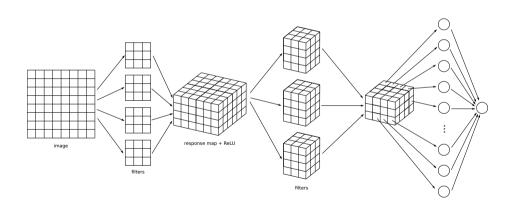
- ► 3-channel 32 × 32 color images
- ▶ 10,000 training images; 2,000 test¹
- ► Cars, trucks in different orientations, scales
- ▶ Balanced: 50% cars, 50% trucks

¹CIFAR-10

Approach #1: Least Squares Classifier

- Train directly on raw features (grayscale)
- Result: 72% train accuracy, 63% test accuracy
- Need a better feature representation

Approach #2: Convolutional Neural Network



Architecture

- ▶ 3 convolutional layers with 32, 64, 64 filters
- ReLU, max pooling after first two
- Dense layer with 64 hidden neurons, ReLU
- Output layer with sigmoid activation
- Minimize cross-entropy loss; use dropout

The Code

```
model = keras.models.Sequential()
model.add( keras.layers.Conv2D(32, (7, 7), activation='relu', input_shape=(32, 32, 1)))
model.add(keras.lavers.MaxPooling2D((2, 2)))
model.add(keras.layers.Conv2D(64. (5, 5), activation='relu'))
model.add(keras.lavers.MaxPooling2D((2, 2)))
model.add(keras.layers.Conv2D(64, (3, 3), activation='relu'))
model.add(keras.layers.Flatten())
model.add(keras.layers.Dropout(0.5))
model.add(keras.lavers.Dense(64. activation='relu'))
model.add(keras.lavers.Dense(1. activation='sigmoid'))
```

The Code

```
model.compile(
    optimizer=keras.optimizers.RMSprop(),
    loss=keras.losses.BinaryCrossentropy(),
    metrics=['accuracy']
model.fit(
    X_train,
    v train,
    epochs=30,
    validation_data=(X_test, y_test)
```

▶ 94% train accuracy, 90% test accuracy





truck / car









truck / truck

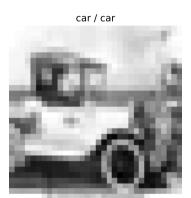


truck / truck



truck / truck







truck / truck



truck / truck



truck / truck



















truck / truck

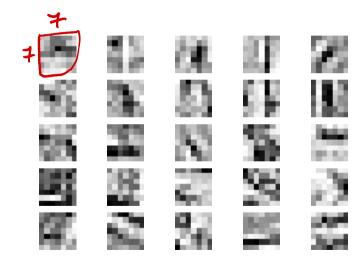








Filters



Next Steps

- In practice, you might not train your own CNN
- Instead, take "pre-trained" convolutional layers from a much bigger network
- Attach untrained fully-connected layer and train
- This is transfer learning