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**Final Exam - DSC 10, Winter 2025**

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Full Name:

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**Instructions:**

- This exam consists of 10 questions, worth a total of 166 points.
  - Write your PID in the top right corner of each page in the space provided.
  - Please write **clearly** in the provided answer boxes; we will not grade work that appears elsewhere. Completely fill in bubbles and square boxes; if we cannot tell which option(s) you selected, you may lose points.
    - ☐ A bubble means that you should only **select one choice**.
    - ☐ A square box means you should **select all that apply**.
  - You may use one page of double-sided handwritten notes. Aside from this, you may not refer to any other resources or technology during the exam. No calculators!
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By signing below, you are agreeing that you will behave honestly and fairly during and after this exam.

Signature:

Version A

Please do not open your exam until instructed to do so.

## Welcome to Hogwarts School of Witchcraft and Wizardry!

Hogwarts is a fictional boarding school from J.K. Rowling's *Harry Potter* book series. Young witches and wizards attend Hogwarts to develop their magical abilities through courses such as Potions, Charms, and Defense Against the Dark Arts.

Hogwarts students belong to one of four living and learning communities called *houses*. These four houses are Gryffindor, Hufflepuff, Ravenclaw, and Slytherin.

The school uses a system of *house points* to encourage good behavior. Through their triumphs and achievements, students can earn points for their house. Likewise, they can lose house points for things like rule-breaking. Faculty can award and deduct these points at their own discretion. At the end of the school year, the house with the most points wins the House Cup, a coveted award.

Throughout this exam, assume we have already run `import babypandas as bpd`, `import numpy as np`, and `import scipy`.

At any point, feel free to use functions and variables that you defined in earlier subparts of the same question.

### Question 1 - A Quidditch Quandary (12 pts)

While browsing the library, Hermione stumbles upon an old book containing game logs for all Quidditch matches played at Hogwarts in the 18th century. Quidditch is a sport played between two houses. It features three types of balls:

- **Quaffle:** Worth 10 points when used to score a goal.
- **Bludger:** Does not contribute points. Instead, used to distract the other team.
- **Snitch:** Worth 150 points when caught. This immediately ends the game.

A game log is a list of actions that occurred during a Quidditch match. Each element of a game log is a two-letter string where the first letter represents the house that performed the action ("G" for Gryffindor, "H" for Hufflepuff, "R" for Ravenclaw, "S" for Slytherin) and the second letter indicates the type of Quidditch ball used in the action ("Q" for Quaffle, "B" for Bludger, "S" for Snitch). For example, "RQ" in a game log represents Ravenclaw scoring with the Quaffle to earn 10 points.

Hermione writes a function, `logwarts`, to calculate the final score of a Quidditch match based on the actions in the game log. The inputs are a game log (a list, as described above) and the full names of the two houses competing. The output is a list of length 4 containing the names of the teams and their corresponding scores. Example behavior is given below.

```
>>> logwarts(["RQ", "GQ", "RB", "GS"], "Gryffindor", "Ravenclaw")
["Gryffindor", 160, "Ravenclaw", 10]
```

```
>>> logwarts(["HB", "HQ", "HQ", "SS"], "Hufflepuff", "Slytherin")
["Hufflepuff", 20, "Slytherin", 150]
```

Fill in the blanks in the `logwarts` function below. Note that some of your answers are **used in more than one place** in the code.

```
def logwarts(game_log, team1, team2):
    score1 = __(a)__
    score2 = __(a)__

    for action in game_log:
        house = __(b)__
        ball = __(c)__

        if __(d)__:
            __(e)__:
                score1 = score1 + 10
            __(f)__:
                score1 = score1 + 150
        else:
            __(e)__:
                score2 = score2 + 10
            __(f)__:
                score2 = score2 + 150
    return [team1, score1, team2, score2]
```

(a):

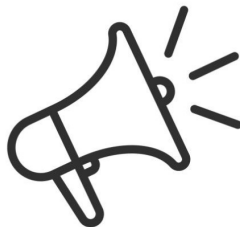
(b):

(c):

(d):

(e):

(f):



***Ten points to  
Gryffindor!***

## Question 2 - Estimating Enemies (13 pts)

The Death Eaters are a powerful group of dark wizards who oppose Harry Potter and his allies. Each Death Eater receives a unique identification number based on their order of initiation, ranging from 1 to  $N$ , where  $N$  represents the total number of Death Eaters.

Your task is to estimate the value of  $N$  so you can understand how many enemies you face. You have a random sample of identification numbers in a DataFrame named `death_eaters` containing a single column called "ID".

- a) (5 pts) Which of the options below would be an appropriate estimate for the total number of Death Eaters? Select all that apply.

- ☐ `death_eaters.get("ID").max()`
- ☐ `death_eaters.get("ID").sum()`
- ☐ `death_eaters.groupby("ID").count()`
- ☐ `int(death_eaters.get("ID").mean() * 2)`
- ☐ `death_eaters.shape[0]`
- ☐ None of the above.

- b) (2 pts) Each box that you selected in part (a) is an example of what?

- ☐ a distribution      ☐ a statistic      ☐ a parameter      ☐ a resample

- c) (6 pts) Suppose you have access to a function called `estimate`, which takes in a Series of Death Eater ID numbers and returns an estimate for  $N$ . Fill in the blanks below to do the following:

- Create an array named `boot_estimates`, containing 10,000 of these bootstrapped estimates of  $N$ , based on the data in `death_eaters`.
- Set `left_72` to the **left endpoint** of a 72% confidence interval for  $N$ .

```
boot_estimates = np.array([])

for i in np.arange(10000):
    boot_estimates = np.append(boot_estimates, __ (a) __)

left_72 = __ (b) __
```

(a):

(b):

**Question 3 - Where Will The Weasleys Wind Up? (16 pts)**

When new students arrive at Hogwarts, they get assigned to one of the four houses (Gryffindor, Hufflepuff, Ravenclaw, Slytherin) by a magical Sorting Hat.

Throughout this problem, we'll assume that the Sorting Hat assigns students to houses uniformly at random, meaning that each student has an independent 25% chance of winding up in each of the four houses.

For all parts, give your answer as an **unsimplified mathematical expression**.

- a) (4 pts) There are seven siblings in the Weasley family: Bill, Charlie, Percy, Fred, George, Ron, and Ginny. What is the probability that all seven of them are assigned to Gryffindor?

- b) (4 pts) What is the probability that Fred and George Weasley are assigned to the same house?

- c) (4 pts) What is the probability that none of the seven Weasley siblings are assigned to Slytherin?

- d) (4 pts) Suppose you are told that none of the seven Weasley siblings is assigned to Slytherin. Based on this information, what is the probability that at least one of the siblings is assigned to Gryffindor?



### Question 4 - Buried Beneath the Bank (10 pts)

Beneath Gringotts Wizarding Bank, enchanted mine carts transport wizards through a complex underground railway on the way to their bank vault.

During one section of the journey to Harry's vault, the track follows the shape of a normal curve, with a peak at  $x = 50$  and a standard deviation of 20.

- a) (4 pts) A ferocious dragon, who lives under this section of the railway, is equally likely to be located anywhere within this region. What is the probability that the dragon is located in a position with  $x \leq 10$  or  $x \geq 80$ ? Select all that apply.

- ☐ `1 - (scipy.stats.norm.cdf(1.5) - scipy.stats.norm.cdf(-2))`
- ☐ `2 * scipy.stats.norm.cdf(1.75)`
- ☐ `scipy.stats.norm.cdf(-2) + scipy.stats.norm.cdf(-1.5)`
- ☐ 0.95
- ☐ None of the above.

- b) (3 pts) Harry wants to know where, in this section of the track, the cart's height is changing the fastest. He knows from his earlier public school education that the height changes the fastest at the **inflection points** of a normal distribution. Where are the inflection points in this section of the track?

- ☐  $x = 50$
- ☐  $x = 20$  and  $x = 80$
- ☐  $x = 30$  and  $x = 70$
- ☐  $x = 0$  and  $x = 100$

- c) (3 pts) Next, consider a different region of the track, where the shape follows some arbitrary distribution with mean 130 and standard deviation 30. We don't have any information about the shape of the distribution, so it is not necessarily normal.

What is the minimum proportion of area under this section of the track within the range  $100 \leq x \leq 190$ ?

- ☐ 0.77
- ☐ 0.55
- ☐ 0.38
- ☐ 0.00

## Question 5 - Fantastic Frog Feast (11 pts)

Among Hogwarts students, Chocolate Frogs are a popular enchanted treat. Chocolate Frogs are individually packaged, and every Chocolate Frog comes with a collectible card of a famous wizard (ex. “Albus Dumbledore”). There are 80 unique cards, and each package contains **one card selected uniformly at random from these 80**.



Neville would love to get a complete collection with all 80 cards, and he wants to know how many Chocolate Frogs he should expect to buy to make this happen.

- a) (4 pts) Suppose we have access to a function called `frog_experiment` that takes no inputs and simulates the act of buying Chocolate Frogs until a complete collection of cards is obtained. The function returns the number of Chocolate Frogs that were purchased. Fill in the blanks below to run 10,000 simulations and set `avg_frog_count` to the average number of Chocolate Frogs purchased across these experiments.

```
frog_counts = np.array([])

for i in np.arange(10000):
    frog_counts = np.append(__(a)__)

avg_frog_count = ____(b)__
```

(a):

(b):

- b) (4 pts) Realistically, Neville can only afford to buy 300 Chocolate Frog cards. Using the simulated data in `frog_counts`, write a Python expression that evaluates to an approximation of the probability that Neville will be able to complete his collection.

- c) (3 pts) **True or False:** The Central Limit Theorem states that the data in `frog_counts` is roughly normally distributed.

☐ True      ☐ False

## Question 6 - Snape's Sneaky Scheme (24 pts)

Professor Severus Snape is rumored to display favoritism toward certain students. Specifically, some believe that he awards more house points to students from **wizarding families** (those with at least one wizarding parent) than students from **muggle families** (those without wizarding parents).

To investigate this claim, you will perform a permutation test with these hypotheses:

- **Null Hypothesis:** Snape awards house points **independently of a student's family background** (wizarding family vs. muggle family). Any observed difference is due to chance.
- **Alternative Hypothesis:** Snape awards **more** house points to students from wizarding families, on average.

*wiz > muggle*

The DataFrame `snape` is indexed by "Student" and contains information on each student's family background ("Family") and the number of house points awarded by Snape ("Points"). The first few rows of `snape` are shown below.

*groupby ('Family')*  
*mean()*  
*M | 7*  
*W | 14*

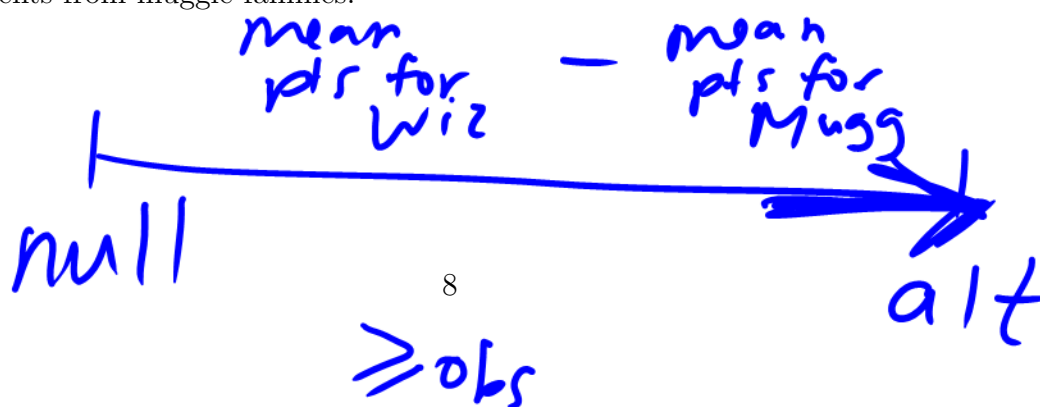
Student	Family	Points
Draco	Wizarding	15
Hermione	Muggle	7
Cho	Wizarding	13

*categories (2)*  
*numerical*

(3 pts) Which of the following is the most appropriate test statistic for our permutation test?

- ☐ The total number of house points awarded to students from wizarding families minus the total number of house points awarded to students from muggle families.
- ☒ The mean number of house points awarded to students from wizarding families minus the mean number of house points awarded to students from muggle families.
- ☐ The number of students from wizarding families minus the number of students from muggle families.
- ☐ The absolute difference between the mean number of house points awarded to students from wizarding families and the mean number of house points awarded to students from muggle families.

*diff of means*





- b) (5 pts) Fill in the blanks in the function `one_stat`, which calculates one value of the test statistic you chose in part (a), based on the data in `df`, which will have columns called "Family" and "Points".

```
def one_stat(df):
    grouped = df.groupby(__(a)__).__(b)__
    return ____(c)__
```

(a):

"Family"

(b):

mean().get('Points')

(c):

grouped.loc['Wizarding'] - grouped.loc['Muggle']

- c) (5 pts) Fill in the blanks in the function `calculate_stats`, which calculates 1000 simulated values of the test statistic you chose in part (a), under the assumptions of the null hypothesis. As before, `df` will have columns called "Family" and "Points".

```
def calculate_stats(df):
    statistics = np.array([])

    for i in np.arange(1000):
        shuffled = df.assign(Points = ____(d)__)
        stat = one_stat(__(e)__)
        statistics = ____(f)__

    return statistics
```

(d):

np.random.permutation(df.get('Points'))

(e):

shuffled

(f):

np.append(statistics, stat)

- d) (6 pts) Fill in the blanks to calculate the p-value of the permutation test, based on the data in `snape`.

```
observed = __(g)___
simulated = __(h)___
p_value = (simulated __(i)___ observed).mean()
```

*np.conf.int(0.025, 0)*

*len(simulated)*

(g): one\_stat(shape)

(h): calculate\_stats(shape)

(i):  $\geq$

- e) (2 pts) Define `mini_snape = snape` take np.arange(3) as shown below.

	Family	Points
Student		
Draco	Wizarding	15
Hermione	Muggle	7
Cho	Wizarding	13

*mini-snape*

Determine the value of the following expression.

`len(calculate_stats(mini_snape))`

1000

- f) (3 pts) With `mini_snape` defined as above, there will be at most three unique values in `calculate_stats(mini_snape)`. What are those three values? Put the **smallest** value on the left and the largest on the right.

-5

-2

7

13, 15

7, 13  
10  
- 15  
-5

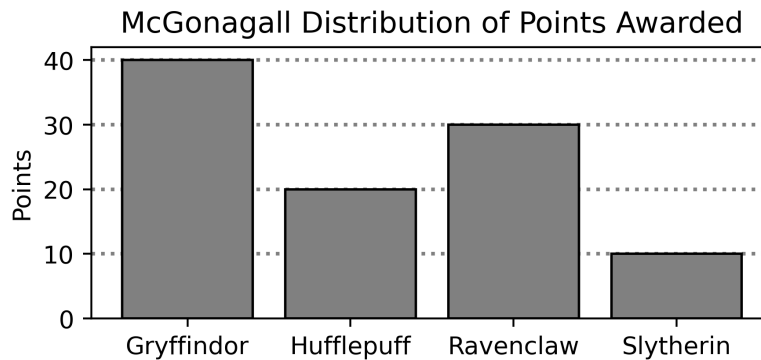
5, 7  
11  
13  
10  
-2

14  
- 7  
7

### Question 7 - Possible Preferential Points? (24 pts)

Professor Minerva McGonagall, head of Gryffindor, may also be awarding house points unfairly. For this question, we'll assume that all four of the houses contain the same number of students, and we'll investigate whether McGonagall awards points equally to all four houses.

Below is the distribution of points that Professor McGonagall awarded during the last academic year.

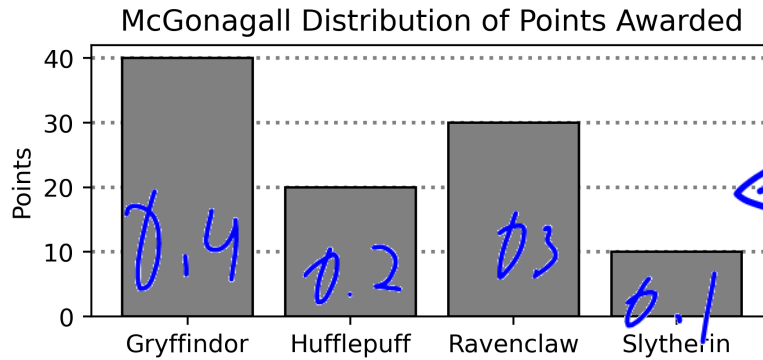


You want to test the following hypotheses:

- **Null Hypothesis:** The distribution of points awarded by Professor McGonagall is uniform across all of the houses.
- **Alternative Hypothesis:** The distribution of points awarded by Professor McGonagall is not uniform across all of the houses.

a) (5 pts) Which of the following test statistics is appropriate for this hypothesis test? Select all that apply.

- ☐ The absolute difference between the number of points awarded to Gryffindor and the proposed proportion of points awarded to Gryffindor. X
- ☒ The difference between the number of points awarded to the house with the most points and the house with the least points. + - alt
- ☐ The sum of the squared differences in proportions between McGonagall's distribution and ~~[0.5, 0.5, 0.5, 0.5]~~. null
- ☐ The sum of the differences in proportions between McGonagall's distribution and [0.25, 0.25, 0.25, 0.25].
- ☒ The sum of the squared differences in proportions between McGonagall's distribution and [0.25, 0.25, 0.25, 0.25].
- ☐ None of the above.



For the rest of this problem, we will use the following test statistic:

The sum of the absolute differences in proportions between McGonagall's distribution and  $[0.25, 0.25, 0.25, 0.25]$ .

- b) (2 pts) Choose the correct way to implement the function `calculate_test_stat`, which takes in two distributions as arrays and returns the value of this test statistic.

```
def calculate_test_stat(dist_1, dist_2):
    return -----
```

- ☐ `np.abs(sum(dist_1 - dist_2))`
☐ `abs(sum(dist_1 - dist_2))`  
☒ `sum(np.abs(dist_1 - dist_2))`
☐ `sum(abs(dist_1 - dist_2))`

- c) (10 pts) Fill in the blanks in the code below so that `simulated_ts` is an array containing 10,000 simulated values of the test statistic under the null. Note that your answer to blank (c) is used in more than one place in the code.

```
mc_gon = np.arange(__(a)__) # Careful: np.arange, not np.array!
null = np.array([0.25, 0.25, 0.25, 0.25])
observed_ts = calculate_test_stat(__(b)__)
```

```
simulated_ts = np.array([])
```

```
for i in np.arange(10000):
    sim = np.random.multinomial(__(c)__, ____(d)__) / ____(c)__
    one_simulated_ts = calculate_test_stat(__(e)__)
    simulated_ts = np.append(simulated_ts, one_simulated_ts)
```

(a):

0.1, 0.5, 0.1

(b):

mc\_gon, null

(c):

100

← how many

(d):

Null

(e):

sim, null

dist choosing from

$p\text{-value} < 0.05 \Rightarrow \text{reject Null}$   
 $p\text{-value} \geq 0.05 \Rightarrow \text{don't reject null}$   
 PID: \_\_\_\_\_  
 d) (4 pts) Fill in the blank so that `reject_null` evaluates to `True` if we reject the null hypothesis at the 0.05 significance level, and `False` otherwise.

`reject_null = __(f)__`

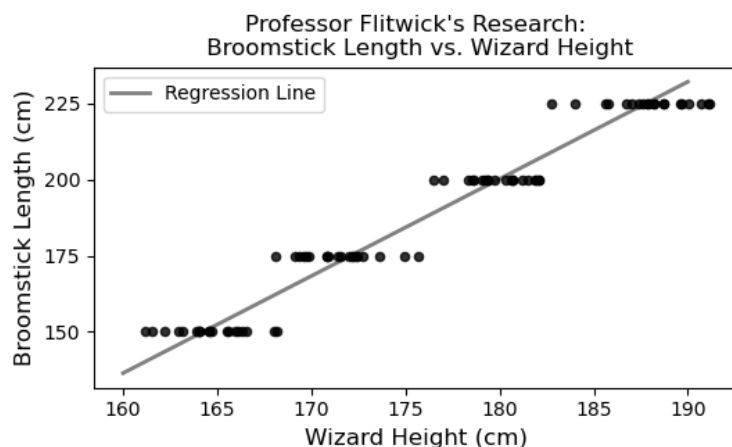
(f): 
$$\frac{\sum (\text{simulated\_ts} - \text{observed\_ts})}{10000} < 0.05$$

e) (3 pts) Your friend performs the same hypothesis test as you, but uses the total variation distance (TVD) as their test statistic instead of the one described in the problem. Which of the following statements is true?

- ☐ Your friend's simulated statistics will be larger than yours, because TVD accounts for the magnitude *and* direction of the differences in proportions.
- ☐ Your friend's simulated statistics will be larger than yours, but **not** because it accounts for the magnitude and direction of the differences in proportions.
- ☐ Your friend's simulated statistics will be smaller than yours, because TVD accounts for the magnitude *and* direction of the differences in proportions.
- ☒ Your friend's simulated statistics will be smaller than yours, but **not** because it accounts for the magnitude and direction of the differences in proportions.
- ☐ There is no relationship between the statistic you used and the statistic your friend used (TVD).

## Question 8 - Regression-Related Research (23 pts)

Professor Filius Flitwick is conducting a study whose results will be used to help new Hogwarts students select appropriately sized broomsticks for their flying lessons. Professor Flitwick measures several wizards' heights and broomstick lengths, both in centimeters. Since broomsticks can only be purchased in specific lengths, the scatterplot of broomstick length vs. height has a pattern of horizontal stripes:



If we group the wizards in Professor Flitwick's research study by their broomstick length, and average the heights of the wizards in each group, we get the following results.

Average Wizard Height (cm)	
Broomstick Length (cm)	
150	165.0
175	172.5
200	180.0
225	187.5

It turns out that the regression line that predicts broomstick length ( $y$ ) based on wizard height ( $x$ ) passes through the four points representing the means of each group. For example, the first row of the DataFrame above means that  $(165, 150)$  is a point on the regression line, as you can see in the scatterplot.

- a) (5 pts) Based only on the fact that the regression line goes through these points, which of the following *could* represent the relationship between the standard deviation of broomstick length ( $y$ ) and wizard height ( $x$ )? Select all that apply.

- ☐  $SD(y) = SD(x)$ 
☐  $SD(y) = 4 \cdot SD(x)$
- ☐  $SD(y) = 2 \cdot SD(x)$ 
☐  $SD(y) = 5 \cdot SD(x)$
- ☐  $SD(y) = 3 \cdot SD(x)$ 
☐ None of the above.

- b) (4 pts) Now suppose you know that  $SD(y) = 3.5 \cdot SD(x)$ . What is the correlation coefficient,  $r$ , between these variables? Give your answer as a **simplified fraction**.

- c) (5 pts) Suppose we convert **all wizard heights** from centimeters to inches (1 inch = 2.54 cm). Which of the following will change? Select all that apply.

- ☐ The standard deviation of wizard heights.
- ☐ The proportion of wizard heights within three standard deviations of the mean.
- ☐ The correlation between wizard height and broom length.
- ☐ The slope of the regression line predicting broom length from wizard height.
- ☐ The slope of the regression line predicting wizard height from broom length.
- ☐ None of the above.

- d) (3 pts) Suppose we convert **all wizard heights and all broomstick lengths** from centimeters to inches (1 inch = 2.54 cm). Which of the following will change, as compared to the original data when both variables were measured in centimeters? Select all that apply.

- ☐ The correlation between wizard height and broom length.
- ☐ The slope of the regression line predicting broom length from wizard height.
- ☐ The slope of the regression line predicting wizard height from broom length.
- ☐ None of the above.

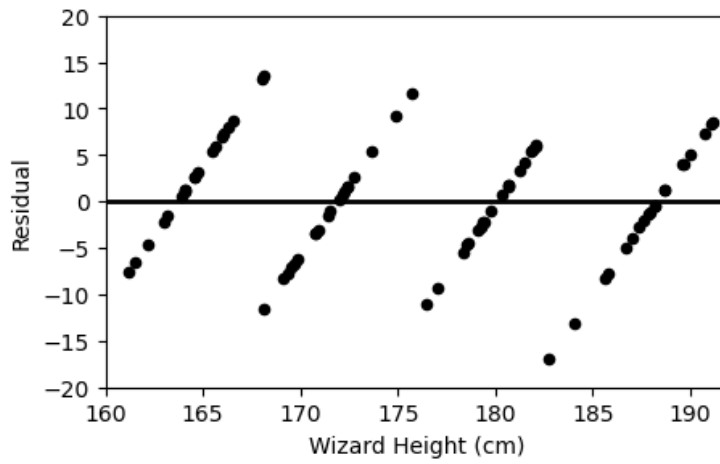
- e) (3 pts) Professor Flitwick calculates the root mean square error (RMSE) for his regression line to be **36 cm**. What does this RMSE value suggest about the accuracy of the regression line's broomstick length predictions?

- ☐ The predictions are, on average, 6 cm off from the actual broomstick lengths.
- ☐ The predictions are, on average, 36 cm off from the actual broomstick lengths.
- ☐ The predictions are, on average,  $(36)^2$  cm off from the actual broomstick lengths.
- ☐ Every wizard's broomstick length differs from the predicted length by 36 cm.
- ☐ The predictions are more accurate for shorter wizards than taller wizards.
- ☐ The RMSE does not tell us anything about prediction accuracy.
- ☐ None of the above.

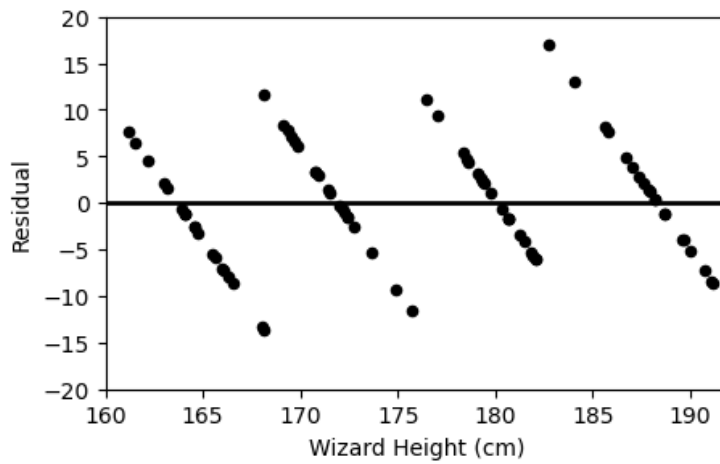


f) (3 pts) Which of the following plots is the residual plot for Professor Flitwick's data?

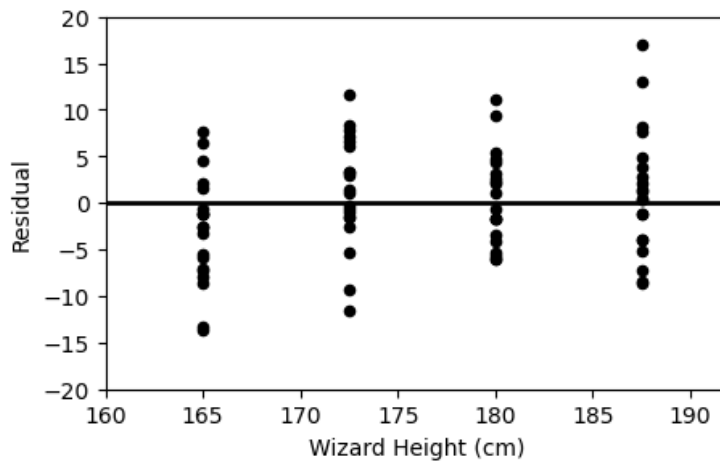
☐ Option A:



☐ Option B:



☐ Option C:





## Question 9 - Triwizard Tournament (22 pts)

The Triwizard Tournament is an international competition between three wizarding academies: Hogwarts, Durmstrang, and Beauxbatons.

In a Triwizard Tournament, wizards from each school compete in three dangerous magical challenges. If one school wins two or more challenges, that school is the **tournament champion**. Otherwise, there is no champion, since each school won a single challenge.

The DataFrame `triwiz` has a row for each challenge from the first 20 Triwizard Tournaments. With 20 tournaments each having 3 challenges, `triwiz` has **exactly 60 rows**. The first six rows are shown below.

	Year	Host	Challenge	Winner
0	1294	Hogwarts	1	Beauxbatons
1	1294	Hogwarts	2	Durmstrang
2	1294	Hogwarts	3	Beauxbatons
3	1299	Durmstrang	1	Beauxbatons
4	1299	Durmstrang	2	Hogwarts
5	1299	Durmstrang	3	Durmstrang

The columns are:

- "Year" (`int`): Triwizard Tournaments are held only once every five years.
- "Host" (`str`): Triwizard Tournaments are held at one of the three participating schools on a rotating basis: Hogwarts, Durmstrang, Beauxbatons, back to Hogwarts again, etc.
- "Challenge" (`int`): Either 1, 2, or 3.
- "Winner" (`str`): The school that won the challenge.

- a) (10 pts) Fill in the blanks below to create the DataFrame `champions`, which is indexed by "Winner" and has just one column, "Year", containing **the number of years in which each school was the tournament champion**. `champions` is shown in full below.

	Year
Winner	
Beauxbatons	4
Durmstrang	5
Hogwarts	5

Note that the values in the "Year" column add up to 14, not 20. That means there were 6 years in which there was a tie (for example, 1299 was one such year).

```
grouped = triwiz.groupby(__(a)__).__(b)__.__(c)__
filtered = grouped[__(d)__]
champions = filtered.groupby(__(e)__).__(f)__.__(g)__
```

(a):

(b):

(c):

(d):

(e):

(f):

(g):

- b) (4 pts) How many rows are in the DataFrame that results from merging `triwiz` with itself on "Year"? Give your answer as an **integer**.

- c) (4 pts) How many rows are in the DataFrame that results from merging `triwiz` with itself on "Challenge"? Give your answer as an **integer**.

- d) (4 pts) How many rows are in the DataFrame that results from merging `triwiz` with itself on "Host"? Select the expression that evaluates to this number.

- ☐  $2 \cdot 6^2 + 7^2$
- ☐  $2 \cdot 7^2 + 6^2$
- ☐  $2 \cdot 18^2 + 21^2$
- ☐  $2 \cdot 21^2 + 18^2$

### Question 10 - Bertie Bott's Bacon Beans (11 pts)

Bertie Bott's Every Flavor Beans are a popular treat in the wizarding world. They are jelly bean candies sold in **boxes of 100 beans**, containing a variety of flavors including chocolate, peppermint, spinach, liver, grass, earwax, and paper. Luna's favorite flavor is bacon.

Luna wants to estimate the proportion of bacon-flavored beans produced at the Bertie Bott's bean factory. She buys a box of Bertie Bott's Every Flavor Beans and finds that **4 of the 100 beans** inside are bacon-flavored. Using this sample, she decides to construct an **86% CLT-based confidence interval** for the proportion of bacon-flavored beans produced at the factory.

- a) (3 pts) Let's begin by solving a related problem that will help us in the later parts of this question. Consider the following fact:

**For a sample of size 100 consisting of 0's and 1's, the maximum possible width of an 86% CLT-based confidence interval is approximately 0.15.**

Use this fact to find the value of  $z$  such that `scipy.stats.norm.cdf(z)` evaluates to 0.07. Give your answer as a **number to one decimal place**.

- b) (4 pts) Suppose that Luna's sample has a standard deviation of 0.2. What are the endpoints of her 86% confidence interval? Give each endpoint as a **number to two decimal places**.

- c) (4 pts) Hermione thinks she can do a better job of estimating the proportion of bacon-flavored beans, though she'll need a bigger sample to do so. Hermione will collect a new sample and use it to construct another 86% confidence interval for the same parameter. Under the assumption that Hermione's sample will have the same standard deviation as Luna's sample, which was 0.2, **how many boxes** of Bertie Bott's Every Flavor Beans must Hermione buy to guarantee that the width of her 86% confidence interval is at most 0.012? Give your answer as an **integer**.

**Remember:** There are 100 beans in each box.

sample prop  
0.04

factory prop  
?

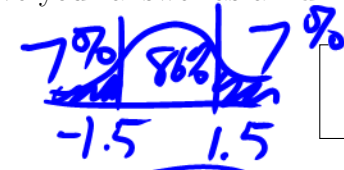
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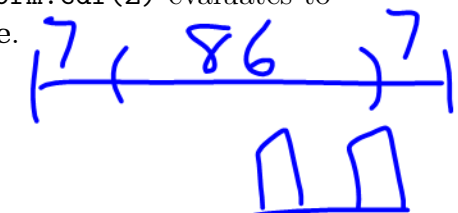
width for 95% CI

$$4 \cdot 0.5 / \sqrt{100} = 0.2$$

max width for 86% CI 0.15

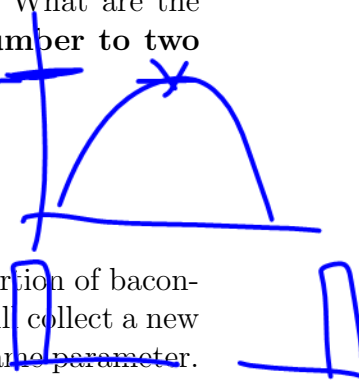


$$-1.5$$



$$\frac{\text{sample SD}}{\sqrt{\text{sample size}}}$$

$$\frac{3 \cdot 0.2}{\sqrt{100}}$$



$$\boxed{\phantom{000}}$$

$$\Rightarrow 0.15 = z \cdot 0.05 \Rightarrow z = 3$$

$$= z \cdot \frac{0.5}{\sqrt{100}}$$

Feel free to draw us a picture or tell us about your fondest memory from DSC 10 this quarter.

A large, empty rectangular box with a thin black border, intended for a student to draw a picture or write about their fondest memory from DSC 10.

Before turning in your exam, please make sure that your PID is on every page.

Congratulations on finishing DSC 10!