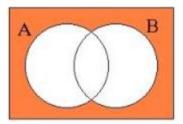
DSC 40A - Extra Practice Session 5

Wednesday, March 2, 2022

Problem 1. Complements of Independent Events are Independent

Let A and B be two independent events in the sample space S. Show that \bar{A} and \bar{B} must be independent of one another.

You may use the fact that $P(\bar{A} \cap \bar{B}) = 1 - P(A \cup B)$, which should be apparent from the Venn diagram below.



Problem 2. Visualizing Independence and Conditional Independence

Let's represent a sample space S as a rectangle with area one. Then we'll represent events within that sample space as regions with area equal to their probability.





disjoint/no Ove/lap

are they

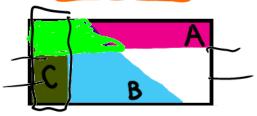
For the sample space S shown below, draw two **independent** events A and B with $P(A) = \frac{1}{4}$ and $P(B) = \frac{2}{3}$.



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In the sample space S shown below, are A and B independent? Are A and B conditionally independent given C?







d) For the sample space S shown below, draw events A, B, and C such that A and B are independent but conditionally dependent given C.



Problem 3.

In parts of the world other than San Diego, the weather changes from day to day. In these places, people try to guess tomorrow's weather using the current conditions.

Weather data for 20 random days in Columbus, Ohio are recorded below, along with the next day's weather (rainy, cloudy, or sunny).

Suppose that today's humidity is > 50%, the temperature is hot, and the air pressure is low. Use Naive Bayes (without smoothing) to predict whether tomorrow will be rainy, cloudy, or sunny. Show your work.

Bayes (without s	smoothing) to predict whe	ther tomorrow	will be rainy, clo		, The state of the
	Next Day's Weather	Humidity	Temperature	Air Pressure	4955
Bayes	Rainy	> 50% > 50% > 50% > 50% 25%-50% 25%-50% 25%-50% < 25% < 25% < 25%	Cool Hot Cool Hot Cool Cool Cool Hot Hot	Low Low High Low Low Low Low Low How High	features
$P(B A) = \frac{P(A B) * P(B)}{P(A)}$	Cloudy Cloudy Cloudy Cloudy Cloudy Cloudy	> 50% > 50% 25%-50% < 25% < 25%	Cool Cool Ho Cool Cool	Low Low High High Low	
	Sunny Sunny Sunny Sunny Sunny Sunny	> 50% > 50% > 50% > 50% 25%-50% < 25%	Cool Hot Cool Hot Hot	Low High High High High	
P(rainy fe	artures) c	LP	- pro (featu	portion restrai	ny) XP(rainy)
b / 1 1 1	,	3	5 * <u>S</u>	× 8	* 20
Y(Cloudy) fe	atures) \propto	()	(featu	res clo	n dy) + P(cloidy)
P(Sumy fe	atures) \sim		Geatu	red sui	n Ny) + P(cluin) n Ny) + P(suray) x 5
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